

MATH 118: Quiz 5

Name: key

Directions:

- * Show your thought process (commonly called "showing your work") when solving each problem for full credit.
- * If you do not know how to solve a problem, try your best and/or explain in English what you would do.
- * Good luck!

1. Suppose

$$f(x) = -2x^2 - x \quad g(x) = 2x + 3x^2 \quad h(x) = 3x - 2 \quad k(x) = 2 - 3x$$

Evaluate and simplify the following:

$$\begin{aligned} \text{(a) } f(x) - 2g(x) &= -2x^2 - x - 2(2x + 3x^2) \\ &= -2x^2 - x - 4x - 6x^2 \\ &= -8x^2 - 5x = \boxed{-x(8x + 5)} \end{aligned}$$

(b) $h \circ f$

$$\begin{aligned} (h \circ f)(x) &= h(f(x)) = h(-2x^2 - x) = 3(-2x^2 - x) - 2 \\ &= \boxed{-6x^2 - 3x - 2} \end{aligned}$$

(c) $k \circ k$

$$\begin{aligned} (k \circ k)(x) &= k(k(x)) = k(2 - 3x) = 2 - 3(2 - 3x) \\ &= 2 - 6 + 9x = \boxed{9x - 4} \end{aligned}$$

(d) $\frac{-h(x)}{k(x)}$

$$\begin{aligned} &= \frac{-(3x - 2)}{2 - 3x} = \frac{-3x + 2}{2 - 3x} = \frac{2 - 3x}{2 - 3x} = \boxed{1} \end{aligned}$$

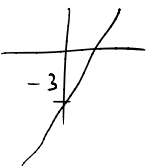
2. Consider $g(x) = -2 - 3\sqrt{-2x + 4}$. Identify each transformation and the order you would apply them in to transform the parent $f(x) = \sqrt{x}$ into $g(x)$.

$$g(x) = -2 - 3\sqrt{-2x + 4}$$

$$= -2 - 3\sqrt{-2(x - 2)}$$

(1) reflection around x-axis
 (2) reflection around y-axis
 (3) v stretch by factor of 3
 (4) h shrink by factor of $\frac{1}{2}$
 (5) v shift down 2 units
 (6) h shift right 2 units

3. Find the inverse of the function $f(x) = 2x - 5$, if possible.

(1) graph  one-to-one ✓

(2) $y = 2x - 5$

(4) $y = \frac{x + 5}{2}$

(3) $y + 5 = 2x$
 $x = \frac{y + 5}{2}$

$$f^{-1}(x) = \frac{x + 5}{2}$$